## Exercise 14

The graph (from the US Department of Energy) shows how driving speed affects gas mileage. Fuel economy $F$ is measured in miles per gallon and speed $v$ is measured in miles per hour.
(a) What is the meaning of the derivative $F^{\prime}(v)$ ?
(b) Sketch the graph of $F^{\prime}(v)$.
(c) At what speed should you drive if you want to save on gas?


## Solution

The value of $F^{\prime}$ is the slope of the tangent line to $F$ at each value of $v$, and it represents the increase in miles per gallon by going a little bit faster.


To save on gas, you should drive at speeds where the graph has the highest value, that is, at about 50 miles per hour.

Below is a better scaled graph of $F^{\prime}(v)$ versus $v$.


